# Elementary Statistics 



## Pioturing



Larson

This page intentionally left blank

# Elementary Statistics PICTURING THE WORLD 

Ron Larson

The Pennsylvania State University
The Behrend College

Content Development: Robert Carroll
Content Management: Suzanna Smith-Bainbridge, Amanda Brands Moschberger
Content Production: Noelle Saligumba, Peggy McMahon
Product Management: Karen Montgomery
Product Marketing: Demetrius Hall
Rights and Permissions: Tanvi Bhatia/Anjali Singh
Please contact https://support.pearson.com/getsupport/s/ with any queries on this content
Cover images by Shutterstock.
Copyright © 2023, 2019, 2015 by Pearson Education, Inc. or its affiliates, 221 River Street, Hoboken, NJ 07030. All Rights Reserved. Manufactured in the United States of America. This publication is protected by copyright, and permission should be obtained from the publisher prior to any prohibited reproduction, storage in a retrieval system, or transmission in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise. For information regarding permissions, request forms, and the appropriate contacts within the Pearson Education Global Rights and Permissions department, please visit www.pearsoned.com/permissions/. Acknowledgments of third-party content appear on page P1, which constitutes an extension of this copyright page.

PEARSON, ALWAYS LEARNING, and MYLAB are exclusive trademarks owned by Pearson Education, Inc. or its affiliates in the U.S. and/or other countries.

Unless otherwise indicated herein, any third-party trademarks, logos, or icons that may appear in this work are the property of their respective owners, and any references to third-party trademarks, logos, icons, or other trade dress are for demonstrative or descriptive purposes only. Such references are not intended to imply any sponsorship, endorsement, authorization, or promotion of Pearson's products by the owners of such marks, or any relationship between the owner and Pearson Education, Inc., or its affiliates, authors, licensees, or distributors.

Library of Congress Control Number: 2021921349
ScoutAutomatedPrintCode

Pearson's Commitment to Diversity, Equity, and Inclusion
Pearson is dedicated to creating bias-free content that reflects the diversity of all learners. We embrace the many dimensions of diversity, including but not limited to race, ethnicity, gender, socioeconomic status, ability, age, sexual orientation, and religious or political beliefs.
Education is a powerful force for equity and change in our world. It has the potential to deliver opportunities that improve lives and enable economic mobility. As we work with authors to create content for every product and service, we acknowledge our responsibility to demonstrate inclusivity and incorporate diverse scholarship so that everyone can achieve their potential through learning. As the world's leading learning company, we have a duty to help drive change and live up to our purpose to help more people create a better life for themselves and to create a better world.

Our ambition is to purposefully contribute to a world where:

- Everyone has an equitable and lifelong opportunity to succeed through learning.
- Our educational products and services are inclusive and represent the rich diversity of learners.
- Our educational content accurately reflects the histories and experiences of the learners we serve.
- Our educational content prompts deeper discussions with students and motivates them to expand their own learning (and worldview).

We are also committed to providing products that are fully accessible to all learners. As per Pearson's guidelines for accessible educational Web media, we test and retest the capabilities of our products against the highest standards for every release, following the WCAG guidelines in developing new products for copyright year 2022 and beyond. You can learn more about Pearson's commitment to accessibility at https://www.pearson.com/us/accessibility.html.

While we work hard to present unbiased, fully accessible contact, we want to hear from you about any concerns or needs with this Pearson product so that we can investigate and address them.

- Please contact us with concerns about any potential bias at https://www.pearson.com/report-bias.html.
- For accessibility-related issues, such as using assistive technology with Pearson products, alternative text requests, or accessibility documentation, email the Pearson Disability Support team at disability.support@pearson.com.

This page intentionally left blank

## PART 1 DESCRIPTIVE STATISTICS

## 1 Intoduction to Staisitics


$\leftrightarrows$ Where You've Been 4 Where You're Going ..... 1
1.1 An Overview of Statistics 2
1.2 Data Classification 9
Case Study: Reputations of Companies in the U.S. 16
1.3 Data Collection and Experimental Design ..... 17
Activity: Random Numbers 27
Uses and Abuses: Statistics in the Real World 28
Chapter Summary
Review Exercises ..... 30
Chapter Quiz ..... 32
Chapter Test 33
Real Statistics-Real Decisions: Putting it all together 34
History of Statistics-Timeline 3 ..... 35
Technology: Using Technology in Statistics ..... 36
2 Descriptive Statistics ..... 38
J Where You've Been $\quad \rightarrow$ Where You're Going ..... 39
2.1 Frequency Distributions and Their Graphs ..... 40
2.2 More Graphs and Displays ..... 55
2.3 Measures of Central Tendency ..... 67
Activity: Mean Versus Median 81
2.4 Measures of Variation 82
Activity: Standard Deviation ..... 100
Case Study: Business Size 10
2.5 Measures of Position ..... 102
Uses and Abuses: Statistics in the Real World 11 ..... 114
Chapter Summary ..... 115
Review Exercises ..... 116
Chapter Quiz ..... 120
Chapter Test ..... 121
Real Statistics-Real Decisions: Putting it all together ..... 122
Technology: Parking Tickets ..... 123
Using Technology to Determine Descriptive Statistics ..... 124
Cumulative Review: Chapters 1 \& 2 ..... 126

## PART 2 PROBABILITY AND PROBABILITY DISTRIBUTIONS




## PART 3 STATISTICAL INFERENCE



## confidence intervals 296

$\longrightarrow$ Where You've Been $\longrightarrow$ Where You're Going 297
6.1 Confidence Intervals for the Mean ( $\boldsymbol{\sigma}$ Known) 298
6.2 Confidence Intervals for the Mean ( $\boldsymbol{\sigma}$ Unknown) 310

Activity: Confidence Intervals for a Mean 318
Case Study: Marathon Training 319
6.3 Confidence Intervals for Population Proportions 320

Activity: Confidence Intervals for a Proportion 329
6.4 Confidence Intervals for Variance and Standard Deviation 330

Uses and Abuses: Statistics in the Real World 336
Chapter Summary 337
Review Exercises 338
Chapter Quiz 340
Chapter Test 341
Real Statistics-Real Decisions: Putting it all together 342
Technology: United States Foreign Policy Polls 343
Using Technology to Construct Confidence Intervals 344


## 8



## Hypothesis Testing with Two Samples ${ }_{\text {st }}$ <br> Where You've Been $\longrightarrow$ Where You're Going 417

8.1 Testing the Difference Between Means (Independent Samples, $\boldsymbol{\sigma}_{1}$ and $\boldsymbol{\sigma}_{2}$ Known) 418
8.2 Testing the Difference Between Means (Independent Samples, $\boldsymbol{\sigma}_{1}$ and $\boldsymbol{\sigma}_{2}$ Unknown) 428

Case Study: How Protein Affects Weight Gain in Overeaters 436
8.3 Testing the Difference Between Means (Dependent Samples) 437
8.4 Testing the Difference Between Proportions 447

Uses and Abuses: Statistics in the Real World 454
Chapter Summary 455
Review Exercises 456
Chapter Quiz 460
Chapter Test 461
Real Statistics-Real Decisions: Putting it all together 462
Technology: Tails over Heads 463
Using Technology to Perform Two-Sample Hypothesis Tests 464
Cumulative Review: Chapters 6-8 466

## PART 4 MORE STATISTICAL INFERENCE



## Correlation and Regression 468

Where You've Been $\longrightarrow$ Where You're Going 469

9.1 Correlation 470

Activity: Correlation by Eye 485
9.2 Linear Regression 486

Activity: Regression by Eye 496
Case Study: Correlation of Body Measurements 497
9.3 Measures of Regression and Prediction Intervals 498
9.4 Multiple Regression 509

Uses and Abuses: Statistics in the Real World 514
Chapter Summary 515
Review Exercises 516
Chapter Quiz 520
Chapter Test 521
Real Statistics-Real Decisions: Putting it all together 522
Technology: Nutrients in Breakfast Cereals 523
10 Chi-Square Tests and the F-Vistribution ${ }_{s 4}$


10.1 Goodness-of-Fit Test 526
10.2 Independence 536

Case Study: Food Safety Survey 548
10.3 Comparing Two Variances 549
10.4 Analysis of Variance 558

Uses and Abuses: Statistics in the Real World 570
Chapter Summary 571
Review Exercises 572
Chapter Quiz 576
Chapter Test 577
Real Statistics-Real Decisions: Putting it all together 578
Technology: Teacher Salaries 579
Cumulative Review: Chapters 9 \& 10580

## Appendices

APPENDIX A Alternative Presentation of the Standard Normal Distribution A1Standard Normal Distribution Table (0-to-z) A1Alternative Presentation of the Standard Normal Distribution A2APPENDIX B Tables ..... A7
Table 1 Random Numbers A7
Table 2 Binomial Distribution A8
Table 3 Poisson Distribution A11
Table 4 Standard Normal Distribution A16
Table 5 t-Distribution A18
Table 6 Chi-Square Distribution A19
Table 7 F-Distribution A20
Table 8 Critical Values for the Sign Test A25
Table 9 Critical Values for the Wilcoxon Signed-RankTest A25
Table 10 Critical Values for the Spearman Rank Correlation Coefficient A26
Table 11 Critical Values for the Pearson Correlation Coefficient A26
Table 12 Critical Values for the Number of Runs ..... A27
APPENDIX C Normal Probability Plots ..... A28
APPENDIX D Key Formulas ..... A31
Answers to the Try It Yourself Exercises A35
Answers to the Odd-Numbered Exercises A44
Index 11
Credits P1

Welcome to Elementary Statistics: Picturing the World, Eighth Edition. You will find that this textbook is written with a balance of rigor and simplicity. It combines step-by-step instructions, real-life examples and exercises, carefully developed features, and technology that makes statistics accessible to all.

I am grateful for the overwhelming acceptance of the first seven editions. It is gratifying to know that my vision of combining theory, pedagogy, and design to exemplify how statistics is used to picture and describe the world has helped students learn about statistics and make informed decisions.

## What's New in This Edition

The goal of the Eighth Edition was a thorough update of the key features, examples, and exercises:
Examples This edition has 213 examples, nearly $50 \%$ of which are new or revised. Also, several of the examples now show an alternate solution or a check using technology.
Try It Yourself Over $40 \%$ of the 213 Try It Yourself exercises are new or revised.
Picturing the World Over $70 \%$ of these are new or revised. Screen Displays In the examples, technology tips, and other features that show screen displays from Minitab ${ }^{\circledR}$, Excel ${ }^{\circledR}$, the TI-84 Plus, and StatCrunch ${ }^{\oplus}$, the displays were revised as appropriate to make them more visually appealing, easy to follow, and reflective of the most up-to-date version of the software.
Exercises Over 30\% of the more than 2300 exercises are new or revised.
Extensive Chapter Feature Updates A full $50 \%$ of the following key features are new or revised, making this edition fresh and relevant to today's students:

- Where You've Been and Where You're Going
- Uses and Abuses: Statistics in the Real World
- Real Statistics-Real Decisions: Putting it all together
- Chapter Technology Project

References to Co-Requisite Help Margin notes have been included at point-of-use locations throughout this edition to remind students that they can get help reviewing a particular area of mathematics in the Integrated Review in MyLab Statistics.
Applet Activities Revisions have been made to the applet activities throughout the text to reflect changes to the corresponding online applets they reference. Applet activities are discussed further on the next page.
Study Strategies At the bottom of each chapter summary page in Chapters 1 through 10, there are study strategies that students can use to help improve their performance in college. These include tips on improving reading skills, avoiding procrastination, preparing for a test, taking notes, and other areas.

## Features of the Eighth Edition Guiding Student Learning

Where You've Been and Where You're Going Each chapter begins with a two-page visual description of a real-life problem. Where You've Been connects the chapter to topics learned in earlier chapters. Where You're Going gives students an overview of the chapter.
What You Should Learn Each section is organized by learning objectives, presented in everyday language in What You Should Learn. The same objectives are then used as subsection titles throughout the section.
Definitions and Formulas are clearly presented in easy-to-locate boxes. They are often followed by Guidelines, which explain In Words and In Symbols how to apply the formula or understand the definition.
Margin Features help reinforce understanding:

- Study Tips show how to read a table, interpret a result, help drive home an important interpretation, or connect different concepts.
- Tech Tips show how to use Minitab, Excel, the TI-84 Plus, or StatCrunch to solve a problem.
- References to Co-Requisite Help point students to extra math help.
- Picturing the World is a "mini case study" in each section that illustrates the important concept or concepts of the section. Each Picturing the World concludes with a question and can be used for general class discussion or group work. The answers to these questions are included in the Annotated Instructor's Edition.


## Examples and Exercises

Examples Every concept in the text is clearly illustrated with one or more step-by-step examples. Most examples have an interpretation step that shows the student how the solution may be interpreted within the real-life context of the example and promotes critical thinking and writing skills. Each example, which is numbered and titled for easy reference, is followed by a similar exercise called Try It Yourself so students can immediately practice the skill learned. The answers to these exercises are in the back of the book and the worked-out solutions are available in MyLab Statistics in the Student Solutions Manual.
Technology Examples Many sections contain an example that shows how technology can be used to calculate formulas, perform tests, or display data. Screen displays from Minitab, Excel, the TI-84 Plus, and StatCrunch are shown. Additional screen displays are presented at the ends of selected chapters, and detailed instructions are given in separate technology manuals available with the book.
Exercises The exercises give students practice in performing calculations, making decisions, providing explanations, and applying results to a real-life setting. The section exercises are divided into three parts:

- Building Basic Skills and Vocabulary are short-answer, true-or-false, and vocabulary exercises carefully written to nurture student understanding.
- Using and Interpreting Concepts are skill or word problems that move from basic skill development to more challenging and interpretive problems.
- Extending Concepts go beyond the material presented in the section. They tend to be more challenging and are not required as prerequisites for subsequent sections.
Technology Answers Answers in the back of the book are found using calculations by hand and by tables. Answers found using technology (usually the TI-84 Plus) are also included when there are discrepancies due to rounding.


## Review and Assessment

Chapter Summary Each chapter concludes with a Chapter Summary that answers the question What did you learn? The objectives listed are correlated to Examples in the section as well as to the Review Exercises.
Chapter Review Exercises A set of Review Exercises follows each Chapter Summary. The order of the exercises follows the chapter organization. Answers to all odd-numbered exercises are given in the back of the book.
Chapter Quizzes Each chapter has a Chapter Quiz. The answers to all quiz questions are provided in the back of the book. For additional help, see the step-by-step video solutions available in MyLab Statistics.
Chapter Tests Each chapter has a Chapter Test. The questions are in random order. The answers to all test questions are provided in the Annotated Instructor's Edition.
Cumulative Review There is a Cumulative Review after Chapters 2, 5, 8, and 10. Exercises in the Cumulative Review are in random order and may incorporate multiple ideas. Answers to all odd-numbered exercises are given in the back of the book.

## Statistics in the Real World

Uses and Abuses: Statistics in the Real World Each chapter discusses how statistical techniques should be used, while cautioning students about common abuses. The discussion includes ethics, where appropriate. Exercises help students apply their knowledge.
Applet Activities Selected sections contain activities that encourage interactive investigation of concepts in the lesson with exercises that ask students to draw conclusions. The applets are available in MyLab Statistics and at www.pearson.com/math-stats-resources.
Chapter Case Study Each chapter has a full-page Case Study featuring actual data from a real-world context and questions that illustrate the important concepts of the chapter.
Real Statistics—Real Decisions: Putting it all together This feature encourages students to think critically and make informed decisions about real-world data. Exercises guide students from interpretation to drawing of conclusions.
Chapter Technology Project Each chapter has a Technology project using Minitab, Excel, and the TI-84 Plus that gives students insight into how technology is used to handle large data sets or real-life questions.

## Continued Strong Pedagogy from the Seventh Edition

Versatile Course Coverage The table of contents was developed to give instructors many options. For instance, the Extending Concepts exercises, applet activities, Real StatisticsReal Decisions, and Uses and Abuses provide sufficient content for the text to be used in a two-semester course. More commonly, I expect the text to be used in a three-credit semester course or a four-credit semester course that includes a lab component. In such cases, instructors will have to pare down the text's 46 sections.
Graphical Approach As with most introductory statistics texts, this text begins the descriptive statistics chapter (Chapter 2) with a discussion of different ways to display data graphically. A difference between this text and many others is that it continues to incorporate the graphical display of data throughout the text. For example, see the use of stem-and-leaf plots to display data on page 387 . This emphasis on graphical displays is beneficial to all students, especially those utilizing visual learning strategies.
Balanced Approach The text strikes a balance among computation, decision making, and conceptual understanding. I have provided many Examples, Exercises, and Try It Yourself exercises that go beyond mere computation.
Variety of Real-Life Applications I have chosen real-life applications that are representative of the majors of students taking introductory statistics courses. I want statistics to come alive and appear relevant to students so they understand the importance of and rationale for studying statistics. I wanted the applications to be authentic-but they also need to be accessible. See the Index of Applications on page xvi.
Data Sets and Source Lines The data sets in the book were chosen for interest, variety, and their ability to illustrate concepts. Most of the $\mathbf{2 5 0}$-plus data sets contain real data with source lines. The remaining data sets contain simulated data that are representative of real-life situations. All data sets containing 20 or more entries are available in a variety of formats in MyLab ${ }^{\mathrm{TM}}$ Statistics or at www.pearson.com/math-stats-resources. In the exercise sets, the data sets that are available electronically are indicated by the icon.
Flexible Technology Although most formulas in the book are illustrated with "hand" calculations, I assume that most students have access to some form of technology, such as Minitab, Excel, StatCrunch, or the TI-84 Plus. Because technology varies widely, the text is flexible. It can be used in courses with no more technology than a scientific calculator-or it can be used in courses that require sophisticated technology tools. Whatever your use of technology, I am sure you agree with me that the goal of the course is not computation. Rather, it is to help students gain an understanding of the basic concepts and uses of statistics.
Prerequisites Algebraic manipulations are kept to a minimum -often I display informal versions of formulas using words in place of or in addition to variables.
Choice of Tables My experience has shown that students find a cumulative distribution function (CDF) table easier to use than a " 0 -to- $z$ " table. Using the CDF table to find the area under the standard normal curve is a topic of Section 5.1 on
pages 237-241. Because some teachers prefer to use the " 0 -to- $z$ " table, an alternative presentation of this topic is provided in Appendix A.
Page Layout Statistics instruction is more accessible when it is carefully formatted on each page with a consistent open layout. This text is the first college-level statistics book to be written so that, when possible, its features are not split from one page to the next. Although this process requires extra planning, the result is a presentation that is clean and clear.

## Meeting the Standards

MAA, AMATYC, NCTM Standards This text answers the call for a student-friendly text that emphasizes the uses of statistics. My goal is not to produce statisticians but to produce informed consumers of statistical reports. For this reason, I have included exercises that require students to interpret results, provide written explanations, find patterns, and make decisions.
GAISE Recommendations Funded by the American Statistical Association, the Guidelines for Assessment and Instruction in Statistics Education (GAISE) Project developed six recommendations for teaching introductory statistics in a college course. These recommendations are:

- Emphasize statistical literacy and develop statistical thinking.
- Use real data.
- Stress conceptual understanding rather than mere knowledge of procedures.
- Foster active learning in the classroom.
- Use technology for developing conceptual understanding and analyzing data.
- Use assessments to improve and evaluate student learning.

The examples, exercises, and features in this text embrace all of these recommendations.

## MyLab Statistics Resources for Success

MyLab Statistics is available to accompany Pearson's market-leading text options, including Elementary Statistics: Picturing The World, 8e (access code required).
$\mathrm{MyLab}^{\mathrm{TM}}$ is the teaching and learning platform that empowers you to reach every student. MyLab Statistics combines trusted author content-including full eText and assessment with immediate feedback - with digital tools and a flexible platform to personalize the learning experience and improve results for each student. Integrated with StatCrunch ${ }^{\circledR}$, a web-based statistical software program, students learn the skills they need to interact with data in the real world.
MyLab Statistics supports all learners, regardless of their ability and background, to provide an equal opportunity for success. Accessible resources support learners for a more equitable experience no matter their abilities. And options to personalize learning and address individual gaps helps to provide each learner with the specific resources they need to achieve success.

## Student Resources

Each student learns at a different pace. Personalized learning pinpoints the precise areas where each student needs practice, giving all students the support they need - when and where they need it-to be successful.
StatCrunch ${ }^{\circledR}$ is integrated directly into MyLab Statistics. StatCrunch ${ }^{\circledR}$ is a powerful web-based statistical software that allows users to perform complex analyses, share data sets, and generate compelling reports of their data. The vibrant online community offers tens of thousands of shared data sets for students to analyze.

- Collect Users can upload their own data to StatCrunch or search a large library of publicly shared data sets, spanning almost any topic of interest. Data sets from the text and from online homework exercises can also be accessed and analyzed in StatCrunch. An online survey tool allows users to quickly collect data via web-based surveys.
- Crunch A full range of numerical and graphical methods allows users to analyze and gain insights from any data set. Interactive graphics help users understand statistical concepts, and are available for export to enrich reports with visual representations of data.
- Communicate Reporting options help users create a wide variety of visually appealing representations of their data.
StatCrunch can be accessed on your laptop, smartphone, or tablet when you visit the StatCrunch website from your device's browser. For more information, visit the StatCrunch website, or contact your Pearson representative.
Exercises with Immediate Feedback The exercises in MyLab Statistics reflect the approach and learning style of this text, and regenerate algorithmically to give student unlimited opportunity for practice and mastery. Most exercises include learning aids, such as guided solutions and sample problems, and they offer helpful feedback when students enter incorrect answers.
Personalized Homework With Personalized Homework, students take a quiz or test and receive a subsequent homework assignment that is personalized based on their performance. This way, students can focus on just the topics they have not yet mastered.
Integrated Review Elementary Statistics, Picturing the World with Integrated Review can be used in corequisite courses, or simply to help students who enter without a full understanding of prerequisite skills and concepts.
MyLab courses provide the full suite of supporting resources for the Statistics course, plus additional assignments and for study aids from select intermediate algebra topics for students who will benefit from remediation.
Assignments for the integrated review content are pre-assigned in MyLab, making it easier than ever to create your course.
Mindset videos and assignable, open-ended exercises foster a growth mindset in students. This material encourages them to maintain a positive attitude about learning, value their own ability to grow, and view mistakes as learning opportunities - so often a hurdle for math students.

Personal Inventory Assessments are a collection of online exercises designed to promote self reflection and metacognition in students. These 33 assessments include topics such as a Stress Management Assessment, Diagnosing Poor Performance and Enhancing Motivation, and Time Management Assessment.

## Instructor Resources

Your course is unique. So whether you'd like to build your own assignments, teach multiple sections, or set prerequisites, MyLab gives you the flexibility to easily create your course to fit your needs.

## MyLab Features

Performance Analytics enable instructors to see and analyze student performance across multiple courses. Based on their current course progress, the student's performance is identified as above, at, or below expectations through a variety of graphs and visualizations.
Conceptual Question Library There are 1000 questions in the Assignment Manager that require students to apply their statistical understanding.
PowerPoint Presentations include lecture content and key graphics from the textbook. Accessible PowerPoint slides are also available and are built to align with WCAG 2.0 AA standards and Section 508 guidelines.
TestGen ${ }^{\circledR}$ (www.pearsoned.com/testgen) enables instructors to build, edit, print, and administer tests using a computerized bank of questions developed to cover the objectives of the text.
Test Bank features printable PDF containing all the test exercises available in TestGen.
Accessibility Pearson works continuously to ensure our products are as accessible as possible to all students. Currently we work toward achieving WCAG 2.0 AA for our existing products (2.1 AA for future products) and Section 508 standards, as expressed in the Pearson Guidelines for Accessible Educational Web Media (https://www.pearson.com/accessibility-guidelines.html).

## Minitab

Minitab ${ }^{\text {TM }}$ makes learning statistics easy and provide students with a skill-set that is in demand in today's data driven workforce. Bundling Minitab software with educational materials ensures students have access to the software they need in the classroom, around campus, and at home. And having 12-month access to Minitab ensures students can use the software for the duration of their course. ISBN 13: 978-0-13-445640-9 ISBN 10: 0-13-445640-8 (access card only; not sold as stand alone)

## JMP Student Edition

JMP ${ }^{\oplus}$ Student Edition is an easy-to-use, streamlined version of JMP desktop statistical discovery software from SAS Institute, Inc. and is available for bundling with the text. ISBN-13: 978-0-13-467979-2 ISBN-10: 0-13-467979-2

## XLSTAT

XLSTAT ${ }^{\text {TM }}$ is an Excel add-in that enhances the analytical capabilities of Excel. XLSTAT is used by leading businesses and universities around the world. It is available to bundle with this text. For more information, go to www.pearsonhighered.com/xlstat. ISBN-13: 978-0-321-75932-0; ISBN-10: 0-321-75932-X

I owe a debt of gratitude to the many reviewers who helped me shape and refine Elementary Statistics: Picturing the World, Eighth Edition.

## Reviewers of the Current Edition

Chris Bendixen, Lake Michigan College
Seunghee Lee, Pellissippi State Community College
Nancy Liu, Miami Dade College
Lohuwa Mamadu, University of South Florida Ashley Nicoloff, Glendale Community College Jason Samuels, Borough of Manhattan Community College

## Reviewers of the Previous Editions

Rosalie Abraham, Florida Community College at Jacksonville Ahmed Adala, Metropolitan Community College Olcay Akman, College of Charleston Polly Amstutz, University of Nebraska, Kearney John J. Avioli, Christopher Newport University Karen Benway, University of Vermont David P. Benzel, Montgomery College John Bernard, University of Texas - Pan American B.K. Brinkley, Tidewater Community College G. Andy Chang, Youngstown State University Keith J. Craswell, Western Washington University Carol Curtis, Fresno City College Christine Curtis, Hillsborough Community College-Dale Mabry Dawn Dabney, Northeast State Community College Cara DeLong, Fayetteville Technical Community College Ginger Dewey, York Technical College David DiMarco, Neumann College Gary Egan, Monroe Community College Charles Ehler, Anne Arundel Community College Carrie Elledge, San Juan College
Harold W. Ellingsen, Jr., SUNY - Potsdam
Michael Eurgubian, Santa Rosa Jr. College
Jill Fanter, Walters State Community College
Patricia Foard, South Plains College
Douglas Frank, Indiana University of Pennsylvania
Frieda Ganter, California State University
David Gilbert, Santa Barbara City College
Donna Gorton, Butler Community College
Larry Green, Lake Tahoe Community College
Sonja Hensler, St. Petersburg Jr. College
Sandeep Holay, Southeast Community College, Lincoln Campus Lloyd Jaisingh, Morehead State
Nancy Johnson, Manatee Community College
Martin Jones, College of Charleston
David Kay, Moorpark College

Mohammad Kazemi, University of North Carolina-Charlotte Jane Keller, Metropolitan Community College
Susan Kellicut, Seminole Community College
Hyune-Ju Kim, Syracuse University
Rita Kolb, Cantonsville Community College
Rowan Lindley, Westchester Community College
Jeffrey Linek, St. Petersburg Jr. College
Benny Lo, DeVry University, Fremont Diane Long, College of DuPage
Austin Lovenstein, Pulaski Technical College
Rhonda Magel, North Dakota State University
Jason Malozzi, Lower Columbia College
Mike McGann, Ventura Community College
Cynthia McGinnis, Northwest Florida State College
Vicki McMillian, Ocean County College
Lynn Meslinsky, Erie Community College
Larry Musolino, Pennsylvania State University
Lyn A. Noble, Florida Community College at Jacksonville - South Campus
Julie Norton, California State University - Hayward
Lynn Onken, San Juan College
Lindsay Packer, College of Charleston
Nishant Patel, Northwest Florida State
Jack Plaggemeyer, Little Big Horn College
Eric Preibisius, Cuyamaca Community College
Melonie Rasmussen, Pierce College
Cyndi Roemer, Union County College
Neal Rogness, Grand Valley State University
Jean Rowley, American Public University and DeVry University
Elisabeth Schuster, Benedictine University
Jean Sells, Sacred Heart University
John Seppala, Valdosta State University
Carole Shapero, Oakton Community College
Abdullah Shuaibi, Harry S. Truman College
Aileen Solomon, Trident Technical College
Sandra L. Spain, Thomas Nelson Community College
Michelle Strager-McCarney, Penn State-Erie, The Behrend College
Jennifer Strehler, Oakton Community College
Deborah Swiderski, Macomb Community College
William J. Thistleton, SUNY - Institute of Technology, Utica
Millicent Thomas, Northwest University
Agnes Tuska, California State University-Fresno
Clark Vangilder, DeVry University
Ting-Xiu Wang, Oakton Community
Heidi Webb, Horry Georgetown Technical College
Dex Whittinghall, Rowan University
Cathleen Zucco-Teveloff, Rider University

Many thanks to Betsy Farber for her significant contributions to previous editions of the text.
I would also like to thank the staff of Larson Texts, Inc., who assisted with the production of the book. On a personal level, I am grateful to my spouse, Deanna Gilbert Larson, for her love, patience, and support. Also, a special thanks goes to R. Scott O'Neil.

I have worked hard to make this text a clean, clear, and enjoyable one from which to teach and learn statistics. Despite my best efforts to ensure accuracy and ease of use, many users will undoubtedly have suggestions for improvement. I welcome your suggestions.


Ron Larson, odx@psu.edu

Biology and Life Sciences
Adult femur lengths, A30
Adult weights, 67, 68, 69
Age and vocabulary, 482, 483
Ages of dogs, 13
American alligator tail lengths, 127 Bacteria, 495
Birth weights and gestation periods, 260
Black bear weights, 51,341
Black cherry tree volume, 512
Blood types, 130, 155, 160
Body measurements, 497
BRCA1 gene, 153
Brown trout, 218
Calves born on a farm, 191
Cloning, 212
Diameters of white oak trees, 265
Dog lifespan, 565
Elephant weight, 512
Elk population in Pennsylvania, 18
Endangered and threatened species, 573
Eye color, 141, 153
Female body temperature, 271
Female fibula lengths, 50
Female heights, 88, 108, 249
Fijian banded iguana lengths, 53
Fish measurements, 511
Fisher's Iris data set, 60
Flowers, 13
Fork length of yellowfin tuna, 433
Genders of children, 180
Genetics, 144, 213
Gestational lengths of horses, 121
Heights of children, 456
Heights and trunk diameters of trees, 505, 507
Human body temperature, 358, 387
Incubation period for ostrich eggs, 467
Incubation period for swan eggs, 361
Infant crawling age and average monthly temperature, 499
Infant weight, 106
Length and girth of harbor seals, 492
Life spans of fruit flies, 112
Life spans of houseflies, 64
Litter size of Florida panthers, 332
Male body temperature, 271
Male heights, $51,79,88,108$
Mean birth weight, 466
Metacarpal bone length and height of adults, 581
Milk produced by cows, 233
North Atlantic right whale dive duration, 385
Rabbits, 218
Reaction times to auditory stimulus, 52
Rolling a tongue, 180
Salmon swimming, 137, 149

Sex of children, 143
Shoe size and height, 492
Stomach contents of blue crabs, 433
Trimethylamine, 17
Vulnerable, endangered, or critically endangered species, 9
Water footprint for a kilogram of wheat, 258
Weights of boys, 74
Weights of cats, 254
Weights of dogs, 254
Weights of grapefruits, 456
Weights of newborns, 235
Weights of oranges, 456
Weights of teenagers, 258
Weights of toddlers, 317

## Business

Accounting department advisory committee, 171
Advertising sales, 225
Advertising time and sales, 501
Annual revenues, 6
Attracting more customers, 19
Bank employee procedure preference, 542, 546
Bankruptcies, 222
Better Business Bureau complaints, 59
Board of Directors, 176
Book prices, 306
Business executives and selfleadership traits, 153
Cauliflower yield, 512
Cell phone prices, 315, 316
CEO compensations, 31
Charges for satellite television, 118
Company sales, 66
Cost of cellphone repairs, 360
Customer ratings, bed-in-a-box 425
Customer transactions, 433
Distribution of sales, 570
Effectiveness of advertising, 568
Employees and revenue of hotel and gaming companies, 492
Existing home sales, 70
Failure rate of businesses, 216, 217
Farming and agriculture, 289
Fortune 500 companies, 191
Fortune 500 revenues, 30
Gas grill ratings, 411
Gasoline prices, 444, 446
Hotel room rates, 401, 411, 467, 574
Hourly earnings at a consulting firm, 110
Hours spent on calls by a business, 190
Marketing plan, 419
Meal prices at a resort, 411
Milk production, 517, 518
Mobile device repair costs, 315, 316
Monthly sales, 562

Natural gas expenditures, 580
Natural gas marketed productions and exports, 506, 507
Net income of farms, 489
Net profit for Procter \& Gamble, 114
Net sales, 521
New vehicle sales, 506,507
No longer needing a physical store, 32
Number of calls by a business, 190
Numbers of manufacturing businesses, 101
Office positions, 184
Office rental rates, 86, 92
Potato yield, 519
President contract, 32
Prices for computer monitors, 268
Printing company departments, 31
Product ratings, 445
Profit and loss analysis, 199
Rental rates, 122
Repair cost for paint damage, 358
Repair costs for washing machines, 425
Repeat customers, 360
Reputations of companies in the U.S., 16

Response times for customer service representatives, 13
Retail prices of minivans, 456
Retail prices of motorcycles, 456
Sale per customer, 118
Sales for a representative, 52,192 , 193, 194, 195, 530
Sales volumes, 159
Service at electronics store, 33
Shipping errors, 360
Sizes of firms, 180
Smartphone sales, 64
Sorghum yield, 512
Soybean harvest, 26
Starting salaries for Standard \& Poor's companies, 7
Sweet potato yield, 580
Telemarketing and Internet fraud, 578
Telephone sales, 220
Television ratings, 410
Tomato prices, 63
Toothpaste costs, 565
Video game prices, 306
Website costs, 335
Wheat production, 574
Yearly commission earned, 114

## Combinatorics

Access codes, 133, 143, 184
Arranging letters in a word, 175
Birthday problem, 156
Building access code, 185
Code, 169
Committee makeup, 174

Debit card personal identification numbers, 32
Identification number, 139
License plates, 133, 180
Lock box codes, 141
Passwords, 174, 186
Personal identification number, 186
Security code, 174, 183
Sudoku, 168
Telephone numbers, 181

## Computers and Technology

Active users on social networking sites, 63
Battery life of tablets, 360
Byte, 175
Calling a number, 216
Cell phone screen times, $41,43,44$, $45,46,47,48,72$
Collection of personal data by smart speakers, 320,322
Customizing a tablet, 141
Data collected by companies, 290
Data use, 317
Digital device fatigue, 205
Digital device use, 126
Disappearance of Facebook, 282
Going online, 204
Identity theft, 201
Internet access, 182
Internet use, 5
Laptop repairs, 569
Life span of home theater systems, 350, 355
Lifetimes of smartphones, 234
Listening time on a single charge, 384
Mobile payment application users, 34
Online dating app, 328
Phishing, 226
Phone screen sizes, 65
Pinterest, 328
Privacy of personal information, 321
Private internet browsing, 325
Reddit, 221
Reliance on human memory to manage passwords, 291
Robots and computers doing jobs, 409
Smart watch or fitness tracker owners, 33
Snapchat, 328
Social media, 2, 78, 202
Technical failure while working at home, 390
Technology seminar, 183
Testing smartphones, 37
Text messages sent, 55, 56, 57
Time spent checking email, 340
Time spent online, 361
Time spent on social media, 300
Wireless devices, 228
YouTube watching times, 51

## Demographics

Age, 30, 62, 70, 78, 89, 94, 111, 131, $136,138,180,411,482,530$, 532
Age distribution, 142, 163, 293, 572
Annual arrests, 197
Annual income by state, 93
Asthma prevalence by state, 272
Birthdays, 162, 185
Births by day of the week, 535
Bisexual identification, 326
Book reading by U.S. adults, 135
Cell phones per household, 225
Census, 1, 4
Census Bureau geographical regions, 15
Characteristics of people who use yoga and people who do not use yoga, 417, 449, 450
Children per household, 90
Cost of raising a child, 372
Daily activities, 453
Dogs per household, 199
18- to 22-year old U.S. population, 21
Fastest growing U.S. states, 1
Favorite day of the week, 65
Favorite season, 65
Favorite store, 26
Fertility rates by state, 272
Gun ownership, 282
Hiding purchases from spouse or partner, 278
Household food purchasing, 30
Household income, 5, 433, 458, 461, 575
Household sizes, 294
Hunger and homelessness, 325
Immigration, 220
Incomes of adults in Nevada, 7
Level of education, 126, 143
LGBT identification, 326
Life expectancies, 127
Living with a partner, 328
Magazine subscriptions per household, 117
Marital status, 30
Marriage, 213
National identity and birthplace, 327
Nationality, 6, 13
News sources, 323
People who smoke, 145
Per capita disposable income, 291
Per capita milk consumption, 244
Pet ownership, 63, 96
Physician demographics, 33
Population densities of the 50 U.S. states, 288
Population of Iowa, 42
Population of the U.S. by age group, 142
Population of West Ridge County, 21, 22, 23
Populations of counties in Montana, 78
Populations of the 50 U.S. states, 197
Populations of U.S. cities, 9

Providing support to parents, 30
Renters behind on rent payments, 361
Retirement ages, 53
Richest people, 15
Spending on Christmas gifts, 117
States with the greatest numerical population increases, 1
Televisions per household, 119, 198
Top-earning states, 127
Unemployment rates, 117
U.S. population, 1, 229

Value of home and lifespan, 482
Young adults, 452

## Earth Science

Acid rain, 522
Air concentration of fine particulate matter in U.S. cities, 407
Air concentration of nitrogen dioxide in U.S. cities, 407
Air pollution, 32
Archaeology, 93
Archaeology club members, 175
Carbon monoxide levels, 384
Classification of elements, 120
Clear days, 209
Climate change, 294
Cloudy days, 209
Conductivity of river water, 381
Conservation, 273
Cyanide presence in drinking water, 342
Days of rain, 189, 191, 193
Density of elements, 94
Earth's temperature, 406
Greenhouse gases from U.S. energy sources, 287, 288
Hurricanes, 199, 221
Ice thickness, 63
Lead levels, 379, 384
Lightning strikes, 228
Old Faithful eruptions, 46, 96, 273, 472, 475, 477, 480, 488, 489, 499
pH level of river water, 381
pH level of soil, 554
Pollution indices, 116
Precipitation, 6, 12, 221, 335, 426
Protecting the environment, 392
Rain, 140
Snowfall, 197, 270
Sodium chloride concentrations of seawater, 307
Surface concentration of carbonyl sulfide on the Indian Ocean, 287, 288
Temperature, 11, 12, 30, 49, 426
Tornadoes, 127, 306
Water pollution, 175
Water quality, 335
Weather forecasting, 130, 189
Wildland fires, 516
Wind energy, 425
Economics and Finance
Account balance, 77
Allowance, 572

Amount spent at a store, 6
Annual rate of return for large growth mutual funds, 255
ATM cash withdrawals, 54
Broker records, 37
Child support payments, 265
Confidence in U.S. economy, 18
Credit card balance, 77
Credit card debt, 384, 422
Credit card purchases, 113
Credit cards, 193
Credit scores, 460
Crude oil imports, 66
Cryptocurrency, 291
Dow Jones Industrial Average, 272, 442
Earnings and dividends, 483
Electric bill, 118, 575
Federal income tax, 404
Financial plans for retirement, 31
Financial risk managers, 284
Fund assets, 506, 507
Gold prices, 306
Gross domestic product, 376
Gross domestic product and carbon dioxide emissions, 471, 474, 479, 480, 487, 489, 499, 500, 501, 503, 508, 509
Gross domestic product from manufacturing sector, 65
Individual stock price, 145
Investment committee, 177
Loan application approval, 178
Mean utility bill, 96, 108
Money management, 534
Mortgage rates, 317
Popular investment types, 33
Preferences on how to pay for goods, 533
Renewable energy prices, 271
Retirement savings, 5, 152
Savings account, 11
Simulating the stock market, 146
Standard \& Poor's 500, 272
Stock offerings, 504, 507
Stock price, 180, 306, 520
Stock risk, 554
Tax fraud, 325
Tax preparation, 526, 527, 529
Tax refunds, 391
Tax return audits, 229
U.S. trade deficits, 79

Use of a mobile device to manage a bank account, 289
Utility bills, 249

## Education

Abilities in music and mathematics, 153
Academic scholarship, 181
Achievement and school location, 544
ACT composite scores, 250, 289
ACT English score, 426
ACT math score, 8,426
ACT reading score, 286, 426
ACT science score, 426

Actuarial exam, 211
Advanced Dental Admission Test, 258
Ages of college professors, 121
Ages of enrolled students, 303, 308
Ages of high school students, 284
Alumni contributions, 471, 475, 477, 488
Attitudes about safety at schools, 543
Bachelor of Science degree, 7, 30
Bachelor's degrees, 281, 390
Branch campuses, 13
Business degrees, 152
Campus security response times, 50
Chairs in a classroom, 310
Changes needed in U.S. schools, 142
Choosing a college, 545
Class levels, 76
Class project, 175
Class schedule, 180
Class size, 116, 117, 385
College acceptance, 212
College board, 7
College costs, 97, 412
College credits, 75
College debt, 360
College education, 534
College programs, 282
College students and drinking, 229
College students with jobs, 246
College success, 412
College visits, 545
Completing an exam, 197
Continuing education, 544
COVID-19 pandemic impacting ability to complete degree, 126
Dormitory room charges, 118
Earned degrees conferred, 58, 184
Educational attainment, 64, 576
Engineering degrees, 65, 164
Enrollment levels, 185, 225
Exam scores, 63, 225, 334, 418
Expression of political views on college campuses, 281
Extracurricular activities, 350, 355, 356
Faculty classroom hours, 385
Failing a distance learning course, 276, 278
Federal student loans in repayment, 229
Final grade, 77, 78, 510, 511
Freshman orientation, 229
Full-time teaching experience, 573
Getting the classes you want, 142
Grade point averages, $26,33,62,71$, $76,78,98,119,316,471,480$, 514, 563, 569
Grades, 80, 109, 119, 141, 162
GRE scores, 259
High school bell schedule, 14
High school grade point averages and SAT and ACT scores, 32
High school graduation rate, 361, 376
History class grades, 259

History course final presentations, 185
Hours spent on academic activities outside of class, 182
Hours students slept, 225, 264
Hours studying and test scores, 491
Immigrants with bachelor's degrees, 212
International mathematics literacy test scores, 408
Length of a guest lecturer's talk, 109
Library visitation, 30
LSAT scores, 75, 288
Mathematics assessment tests, 401
MCAT scores, 50, 249, 289, 375
Multiple-choice quiz, 202
Music assessment test scores, 460
Music major, 162
New York Grade 6 English Language Arts Operational Test reading subscores, 236
New York Grade 6 Mathematics Operational Test scores, 236
Nursing major, 157
Obstacles that keep students from completing their homework, 25
Off track to graduating because of at least one course failure, 276
Paying for college education, 221, 328, 360,581
Paying for college expenses with a credit card, 268
Physics class students, 162
Plans after high school, 33
Postgraduate degree, 339
Quantitative reasoning scores, 111
Reading assessment test scores, 401, 460
Residency positions, 151
Room and board expense, 267
Room numbers, 14
SAT critical reading scores, 574
SAT French Subject Test, 271
SAT Italian Subject Test, 271
SAT math scores, 4, 200
SAT multiple choice questions, 212
SAT physics scores, 341
SAT reading and writing score, 33
SAT scores, $54,98,106,244,250$, 316, 442, 467, 514
School-related extracurricular activities, 199
Science achievement test scores, 408
Science assessment tests, 556
Standardized test scores, 155
State mathematics test, 430
Statistics course enrollment, 21
Statistics course scores, 78, 121, 183
Student activities and time use, 116
Student daily life, 412
Student living arrangement and borrowing money for college, 537, 540

Student living arrangement and family college experience, 536, 537, 539
Student loans, A29
Student musicians, 197
Students who earn Bachelor of Science or Bachelor of Arts degrees, 447
Students planning to study visual and performing arts, 453
Students in public schools, 182
Students undecided on an intended college major, 453, 461
Study habits, 31
Study hours, 97, 110
Teaching conference, 162
Teaching experience, 295
Teaching load, 97
Teaching methods, 434, 457
Teaching styles, 33
Test scores, 74, 96, 111, 117, 127, 137, 535, 581
Testing times, 121
Texas Bar Exam, 226
Textbook spending, 51
Time spent on homework, 316
Top ten colleges in terms of value for the money, 13
True/false test, 140, 141
Tuition and fees, $75,103,104,105$, $107,385,573$
U.S. history assessment tests, 556

Using social media to research colleges, 155
What Americans know about science, 2

## Engineering

Activating temperature of sprinkler systems, 375
Bolt diameters, 334, 335
Bolt widths, 409
Can defects, 163
Carton defects, 163
Chlorine level in a pool, 399
Circumference of soccer balls, 308
Circumference of tennis balls, 308
Defective disks, 177
Defective DVR, 140
Defective parts, 131, 180, 199, 213, 220, 295
Defective units, 177, 183, 184, 222
Diameter of an engine part, 251
Diameter of a gear, 251
Diameters of machine parts, 270
Fishing line strength, 399
Fossil fuels, 221
Glass manufacturer, 221
Golf ball manufacturing, 394
Injection mold, 575
Juice dispensing machine, 308
Landing an astronaut on Mars, 226
Life of appliances, 555
Life span of a backpack, 361
Life span of lawn mowers, 361
Lifetimes of diamond-tipped cutting tools, 270

Light bulb manufacturing, 317, 376
Liquid dispenser, 251
Liquid volume in cans, 116, 117
Living on Mars, 548
Load-bearing capacities of transmission line insulators, 270
Machine part accuracy, 32
Machine settings, 292
Manufacturing defect, 222
Mean life of a compact fluorescent lamp bulb, 376
Mean life of furnaces, 350, 355
Melting points of industrial lubricants, 270
Milk containers, 272
Nail length, 251
Paint can volumes, 272, 308
Parachute failure rate, 352
Power failures, 75
Solar panels, 6
Speed of sound, 483
Statistical process control, 251
Tennis ball manufacturing, 317
Tensile strength, 433, 434
Testing toothbrushes, 126
Time clocks lose, 360
Volume of gasoline, 191

## Entertainment

Academy Award winners, 112
Albums by The Beatles, 121
American roulette, 200
Amusement park attendance, 360
Arts, 2
Attendance at concerts, 197
Best sellers list, 14
Billboard Hot 100 song lengths, 258
Broadway shows, 15
Celebrities addressing social and political issues, 154
Chess, 360
Comedy series, 13
Fair bet, 199
Finding new music, 176
Game show, 140
Lengths of songs, 113
Live television streaming platforms, 389
Lottery, 142, 173, 175, 176, 178, 211, 222, 226
Monopoly, 148
Motion Picture Association of America ratings, 12
Movie genres, 10
Movie rental late fees, 153
Movies watched in a year, 121
Music, 5
Musical dice game minuet, 187
Number one songs, 75
Planning on summer travel, 320, 322
Raffle, 137, 196, 200
Reading a book, 208, 226
Reviewing a movie, 581
Roller coaster heights, 50, 338, A30
Roller coaster vertical drops, 375
Roulette wheel, 178

Shuffle playback, 176
Singing competition, 175
Song setlist, 175
Spring break destinations, 31
Streaming programming, 389
Television watching, 517, 518
Time The Bachelorette stars stayed with partners, 127
Top-40 radio stations, 119
Top-grossing films, 32
Type of movie rented by age, 543, 546
Types of televised shows, 12
Vacation planning, 14
Video durations, 75
Video game arrangement, 174
Video game scores, 32
Violent video games, 347
Virtual reality device, 210
Winter vacation, 339
Women who are gamers, 360

## Food and Nutrition

Amounts of caffeine in brewed coffee, 97
Caffeine content of soft drinks, 376
Caloric and sodium content of hot dogs, 492
Calorie, fat, carbohydrate, and protein content, 513
Carbohydrates in chicken sandwiches, 557
Carbohydrates in an energy bar, 406
Carbohydrates in a nutrition bar, 411
Cereal boxes, 341
Cholesterol contents of cheese, 307
Cholesterol contents of chicken sandwiches, 557
Coffee consumption, 532
Corn kernel toxin, 173
Eating habits, 25
Eating healthier foods, 26
Eating at a restaurant, 294
Fast food, 326, 376
Fat content in whole milk, 397
Food storage temperature, 4
Grocery shopping, 262
Ice cream, 272
M\&M's, 226, 530, 531
Meal kits, 411
Meal plan choices of college students, 6
Meat and poultry, 392
Menu selection, 141, 175
Nutrients in breakfast cereals, 523
Ordering pizza, 533
Pepper pungencies, 52
Pizza toppings, 176
Protein powder, 79
Restaurant ratings, 542, 546
Restaurant serving times, 409
Restaurant waiting times, 553
Shelf life of dried fruit, 406
Sodium content of sandwiches, 456
Sports drink, 397
Sugar consumption and cavities, 516
Taste test, 53

Temperature of coffee, 312, 313
Vitamin $\mathrm{D}_{3}$ supplementation, 18
Water consumption and weight loss, 481
Weight loss drink, 19
Weight loss supplement, 458
Weights of bags of baby carrots, 259
Whole-grain foods, 26

## Government and Political

## Science

Ages of presidents, 52
Ages of Supreme Court justices, 118
Ages of voters, 137
Asylum decisions, 178
Best president, 154
Brexit, 164
Candidate support, 324
Civil rights, 211
Confidence in elected officials, 69
Congress, 162, 167, 326, 327
Cost of the U.S. Census, 4
Critical threats to the U.S., 327,453
Declaration of Independence, 52
Economic power of China, 343
Election polls, 336
Electoral votes, 6, 64
Eligible voters, 214
Energy situation of the United States, 340
Fake news, 126
Favorable view of Cuba, 7
Foreign trade, 343
Gender profile of Congress, 14
Government salaries, 566, 569
Gun legislation, 282
Israeli-Palestinian conflict, 343
Legislator performance ratings, 440
Perception of police, 282
Political party, 69, 162
Political viewpoints, 164
Position of the United States in the world, 343
President's approval ratings, 23
Problems facing the U.S. today, 206
Registered voter not voting, 143
Registered voters, 6, 8, 37
Republican governors, 8
Senate filibuster, 326, 327
Social Security, 325
Supreme Court approval, 460
Voter opinions, 26
Voter turnout, 506, 507
Votes for Republicans, 143
Worst president, 154
Zoning board, 176

## Health and Medicine

Acne treatment, 25
Age and hours slept, 493
Alcohol and tobacco use, 482
Allergy drug, 333
Anterior cruciate ligament reconstructive surgery, 150
Appetite suppressant, 438
Arthritis medication, 454
Assisted reproductive technology, 155, 230

Attention-defecit/hyperactivity disorder drug, 32
Bacteria vaccine, 28
Blood donors, 157, 175
Blood test, 197
Body mass index, 77, 317
Breast cancer, 28
Bypass surgery, 155
Caffeine consumption and heart attack risk, 536
Cancer drug, 451
Carbon monoxide levels, 6
Cataract surgery patients, 32
Cholesterol levels, 75, 256, 445
Cigarette content, 519
Clinical trial participation, 282
Concussion recovery times, 85, 86
Coronavirus testing, 129
COVID-19 response, 258
COVID-19 vaccine, 227
Danger signs of obstetrics, 31
Days spent at the hospital, 567
Dentist office waiting times, 341
Dieting products and weight loss services, 399
Drug and body temperature, 441
Drug concentration, 334, 335
Drug testing, 446, 448, 459
Drug treatment and nausea, 542, 543
Drug for the treatment of obesity, 349
DVD featuring the dangers of smoking, 20
Eating dark chocolate and heart disease, 404
Emergency department waiting times, 401
Emergency room patients, 79
Epilepsy treatment, 467
Exercise and immunity, 8
Exercising, 26, 120, 541
Experimental group, 175
Eye survey, 165
Feeling well-rested, 7
Gum for quitting smoking, 20
Gut microbiomes of healthy infants, 7

Having trouble sleeping, 159
Headaches and soft tissue massage, 461
Health care reform, 30
Health care visits, 527
Health nonprofit brands, 10
Heart medication, 361
Heart rate and QT interval, 491
Heart rates, 77
Heart transplant waiting times, 556
Height and IQ, 482, 483
Heights and pulse rates, 472
Herbal medicine testing, 446
High blood pressure and cerebral small blood vessel disease, 24
Hospital beds, 78
Hospitals, 54
Hours of sleep, 33, 318, 517, 518
Infant head circumference, 249
Influenza vaccine, 20

Injury recovery, 137
Inpatients length of stay, 462
IQ and brain size, 516
Liver transplant survival rate, 228
Living donor transplants, 221
Loud music and being hard of hearing, 4
Lung cancer, 360
Marijuana use, 163
Mental health and young people, 3
Migraines and injections of onabotulinumtoxinA, 442
Multiple sclerosis drug, 451
Musculoskeletal injury, 543
National Council Licensure Examination, 181
Omega-3 carboxylic acids and reducing the risk of cardiac events, 31
Organ and tissue donation, 7
Pain relievers, 126, 558, 561, 564
People who have survived cancer, 208
Physician's intake form, 15
Physicians involved in patient care, 248
Post-traumatic stress disorder treatment medication, 450
Pregnancy durations, 94, 250, 259
Private health care coverage, 324
Protein and weight gain in overeaters, 436
Pulse rates, 54
Putting off medical treatment, 228
Reaction times to an auditory stimulus, A30
Red blood cell count, 250, 259
Red wine consumption and heart disease prevention, 114
Reducing the number of cigarettes smoked, 454
Resting heart rates, 314
Rotator cuff surgery, 150
Salmonella contamination for ground beef, 352
Saturated fat intakes, 53
Sharing personal health information to advance medical research, 282
Shrimp allergy, 480
Sleep deprivation, 25, 31
Sleep and reaction time, 470
Sleep and student achievement, 8
Smokers, 227
Smoking attitudes, 32
Smoking and emphysema, 148
Spread of infectious diseases, 8
Stem cell research, 23
Surgery success, 130, 202, 203, 275
Surgical treatment, 358
Systolic blood pressure, 64, 234, 418
Talcum powder and the incidence of ovarian cancer, 153
Testing a drug, 283
Therapeutic taping and chronic tennis elbow, 444

Time for nutrients to enter the bloodstream, 553
Training heart rates, 265
Treatment of depression, 75
Triglyceride levels, 53, 418, A30
Trying to quit smoking, 544
Vaccinations, 391
Vaccine reaction, 7
Virus testing, 156
Waiting time to see a family doctor, 435
Weight and hours slept by infants, 508
Weight loss, 8
Weight loss program, 410
Well-being index, 567, 569

## Housing and Construction

Building a new high school, 273
Heights and stories of buildings, 117, 491
Home security alarms, 360
Homes for sale, 91
House size, 350, 355, 357, 535
Housing costs, 234
Indoor temperature at night, 367
Mean construction costs, 314
Mean home sales price, 426, 461
Mean price of new homes, 120
Monthly rent, 423
Predicting house sales, 178
Property inspection, 175
Renting or owning residences, 26
Sales price of an existing home, 267
Sales price of a single-family house, 568
Selling prices of real estate and location, 553
Square footage and home sale price, 491
Subdivision development, 170
Law
Ages and years of experience of lawyers, 119
Custodial sentences, 76
Jury selection, 151, 173, 175, 413
Legal system, 352
Numbers of burglaries, 61
Numbers of robberies, 61
Parking infractions, 273
Police response times, 398
Rezoning a portion of a town, 336
Scores for California Peace Officer Standards and Training test, 255
Supreme Court, 213
Terrorism, 325
Tickets written by a police officer, 225

## Miscellaneous

Affording basic necessities, 361
Animal species and people who own more than two cars in a region, 480
Ban on skateboarding in parks, 33
Beaches, 171

Board positions, 169, 172, 294
Brands of toothpaste and dental rinse, 181
Capacities of commercial freezers, 13
Clothes, 162
Club officers, 176
Coffee beans, 15
Coin and die experiment, 131, 148, 149, 153, 536
Coin and spinner experiment, 139
Coins found on the street, 463
Confidence in newspapers, 211
Cooking area of gas grill, 518
Daylight Savings Time, 227
Die, coin, and spinner experiment, 141
Die and spinner experiment, 143
Dog owners and cat lovers, 181
Drive-thru times, 335
Duck race, 185
Emergency incidents, 223
Floral arrangements, 175, 295
Grocery store checkout counter, 231
Having a gun in the home, 226
Health club costs, 408
Health club schedule, 249
Holding for a telephone call, 231
Hotel room guests, 6
Hurricane relief efforts, 25
Life on other planets, 212
Lumber cutter, 272
Magazine stories, 183
Making a charitable donation, 541
Mean male hat size, 410
Middle names, 141
Months of the year, 180
Moral values, 392
Necklaces, 175
New Year's resolution, 325, 327
News platforms, 14
Obstacle course, 445
Online purchases of eyeglasses, 467
Page counts, 75
Parade floats, 174
Personal protective equipment, 30
Pet food, 432
Phone numbers, 10
Police officer badge numbers, 32
Pronunciation, 211
Random number selection, 24, 27, 36, 140, 141, 142
Rare events, 135
Responsible consumption, 211
Results of a survey, 66
Reviewer ratings, 199
Rock-paper-scissors, 213
Rolling a die, $37,74,79,131,134$, $138,141,142,145,153,157$, $158,159,163,166,180,182$
Rooms reserved at a hotel, 116
Second-hand fashion, 211
Selecting a jelly bean, 181
Selecting a marble, 202
Selecting a numbered ball, 153

Selecting a playing card, 134,141 ,
$145,147,148,149,153,158$, $159,163,173,177,180,181$, 182, 183, 201, 203, 211
Shopping times, 247
Social Security numbers, 10
Sock drawer, 181
Spinning a spinner, 182
Survey, 361
Taking in stray cats, 392
Tattoos, 142
Time spent doing activities, 17
Tossing a coin, $37,136,140,141$,
$148,178,180,181,226,351$
Transferring a telephone call, 398
Typographical errors, 220, 228
Vending machine, 259
Volunteers for an experiment, 25
Wait times, 111
Waiting for an elevator, 231
Weights of vacuum cleaners, 565 , 569
Winning a prize, 145,221
Writing a guarantee, 259
Yoga classes, 66, 408
Zip codes, 13, 30

## Mortality

Deaths caused by falling out of a fishing boat and marriage rate, 482
Drug overdose death rate, 407
Drunk driving fatalities, 93
Fatal pedestrian and bicyclist motor vehicle collisions, 574
Homicide rates and ice cream sales, 482
Homicides by county, 533
Homicides by month, 534
Leading causes of death, 59, 64
Lightning fatalities, 105
Living to age 100,212
Losing a friend or relative to murder, 154
Motor vehicle fatalities, 14, 546
Shark deaths, 227
Tornado deaths, 227

## Motor Vehicles and

Transportation
Acceleration times, 375, 518
Accidents at an intersection, 217, 218
Ages of adults who own motor vehicles, 7
Ages of vehicles, 507
Aggressive driving, 279
Air travel safety, 31
Airplane defects, 119
Alcohol-impaired driving, 326
Alcohol-related accidents, 545
Amount of fuel wasted, 102
Automobile covered warrantee repairs, 142
Automobile parts, 330
Automotive sales, 63
Average speed of vehicles, 246

Base price of an ATV, 360
Bicycle tire pressure, 295
Blood alcohol concentration of drivers, 31
Braking distances, 255, 288, 425, 484
Canadian border ports of entry, 75
Car battery life spans, 295, 350, 355, 357
Car battery reserve capacities, 335
Car colors, 182
Car inspections, 36
Car rental rates, 410
Carbon monoxide emissions, 556
Carpooling, 577
Cars in a parking lot, 197
"Check engine" light, 145
Commute times, 306, 307, 315, 424
Commuting distances, $50,110,315$, 316, 338
Commuting by driving, 207, 283
Commuting by public transportation, 207
Cost per mile for automobiles, 566 , 569
Crash tests, 525
Days cars were on a dealership lot, 313
Department of Motor Vehicles wait times, 382, 384
Diameters of tires, 401
Distance traveled, 26
Driverless car, 32
Driver's license exam, 181
Driving ranges of plug-in hybrid electric vehicles, 76
Electric vehicle for next vehicle purchase, 339
Engine control module, 8
Engine displacement and fuel efficiency, 517, 518
Flight arrivals, 156
Flight departures, 156
Flight prices, 76, 407
Fuel costs of all-electric vehicles, 76
Fuel economy, 80, 119, 456, 519, 563
Gas mileage, 317, 348, 361, 371, 385, 401, 466
Hindenburg airship, 7
Jet fuel use, 228
Least popular drivers, 63
Lengths of automobiles, 14
Life spans of tires, 112, 243
Mean driving cost per mile, 431
Mean listing price of used vehicles sold, 380
Mean price of used cars sold, 384
Mean transaction price of used vehicles sold, 380
Mean vehicle speed, 96, 108
Mileage for a rental car company's fleet, 118
Mileages of service vehicles, 74
Miles driven per day, 266, 267
Motorcycle fuel efficiency, 109
Motorcycle helmet use, 459
Motorcycle speeds, 335

New section of interstate highway, 171
Occupancy of vehicles that travel across a bridge, 218
Oil change time, 350, 355, 356
Oil tankers, 221
Parking infractions and fines, 123
Parking ticket, 153
Pickup trucks, 154
Pilot test, 220
Purchasing extended warranties, 7
Purchasing a new car, 132
Racing car engine horsepowers, 32
Safety driving classes and accidents, 481
Seat belt use, 449, 452
Selecting vehicles, 158
Self-driving vehicle, 147
Simulations with dummies, 18
Space shuttle flight durations, 118, 334
Space travel, 392
Speed and car accidents, 148
Speed of a rocket, 191
Speeds of automobiles, 366
Speeds of powerboats, 424
Texting while driving, 26, 276, 279
Top speeds of sports cars, 62
Towing capacity, 119
Traffic flow rate, 360
Travel time, 361, 385
Truck weight, 225
Type of car owned by gender, 542, 546
Type of car owned by generation, 573
Uninsured drivers, 227
Used cars, 513
Vehicle sales, 568
Vehicle size classes, 30
Vehicle starting prices, 406
Vehicles and crashes, 545
Waiting times to turn left at an intersection, 269
Waiting at a traffic light, 231
Weights of packages on a delivery truck, 76

## Psychology

Attention deficit hyperactivity disorder, 126
Attitudes to mental illness, 31
Child behavior, 454
Contentment with life, 289
Coronavirus pandemic and mental health issues, 164
Dating life, 295
Dating someone of a different religion, 466
Depression and stress, 80
Favorite team's win or loss and mood, 131
Gambler's fallacy, 178
IQ score, 109, 244, 290, 297, 424
Looking up someone online before dating them, 30
Memory retention, 24

Music and body image, 24
Obsessive-compulsive disorder, 546
Online harassment, 76
Parenting attitudes, 7
Parks and mental health, 452
Personality inventory test, 192, 194, 195
Psychological screening test, 418
Psychology experiment, 31, 169
Smoking and vaping cues, 32
Social anxiety disorder, 25
Thoughts about racial inequality, 24
Verbal memory test and musical training, 429
Video games and aggressive or bullying behavior, 153

## Sports

Adult participation in sports, 283
Ages and caps of members of Women's U.S. soccer team, 98
Ages of professional athletes, 566
Ages of Tour de France winners, 112
American League home run totals, 11
Athlete as an occupation, 339
Athletes on social issues, 282
Baseball umpires, 178
Basketball defensive assignments, 183
Basketball 3-pointer, 228
Batting averages, 248, 443
Bench press weights, 424
Big 12 collegiate athletic conference, 168
Body temperatures of athletes, 11
Boston Marathon Open Division champions, 340, 375
Boston Marathon runners' years of birth, 32
Bowling score, 228
Bowling tournament, 184
College football, 15
College football touchdowns, 144
Cycling race, 183
Distance a baseball travels, 197
Distance for holes of a golf course, 80
Distances of track events, 13
Efficiency of a pit crew, 366
Field goals attempted, 339
Figure skating scores, 15
Final standings, National Basketball Association, 10
First serve points won, 221
Football kick distances, 314
Footrace, 175
Former National Football League players and joint replacement surgery, 280
Free throws, 201
Games played in World Series, 199
Goal differential and wins in the English Premier League, 491

Goal production, 227
Goals allowed and points earned in the National Hockey League, 505, 507
Golf driving distances, 435, 556
Golf scores, 360, 439, 440
Golfers, what irritates them most on the golf course, 572
Heart rates of athletes, 11
Heights of basketball players, 65, A29
Heights of volleyball players, 77
Heights and weights of a basketball team, 92
Heights and weights of France national soccer team, 98
Highest-paid athletes, 64
Hits and at-bats, 215
Hits per game, 225
Home gym customer satisfaction rate, 361
Horse race, 176, 226
Indianapolis 500, 169
Lacrosse team, 174
Leisure and sports activities, 4
London Marathon winners, 64
Major League Baseball attendance, $469,472,475,479,480,488$
Major League Baseball salaries, 469, $472,475,479,480,488$
Marathon training, 319
Maximal strength and jump height, 483, 484
Maximal strength and sprint performance, 483, 484
National Football League rookies, 161
NCAA student-athletes having a job waiting for them, 227
New York Yankees' World Series victories, 11
Numbers on sports jerseys, 10
Pass attempts and passing yards, 516
Pass completions, 220
Passing play percentages, 445, 446
Penalty kicks, 211
Penalty shots, 212
Personal fouls per game, 294
Points recorded by Winnipeg Jets, 127
Recovering from a football head injury, 341
Regular season wins for Major League Baseball teams, 120
Runs scored, 96, 458
Soccer goals, 288
Softball team fitted hat sizes, 197
Softball team starting lineup, 174
Speed skating, 174
Sports industry, 409
Sprint interval training, 443
Stretching and injury, 542, 543
Strokes per hole, 222
Student-athletes, 298, 300, 301, 302, 304

Super Bowl points scored, 39, 42, $43,45,46,47,48,56,57,67$, $68,69,72,102,104,105,106$
10K race, 52, 435
Vertical jumps of college basketball players, 117
Volleyball service aces scored, 335
Weightlifting, 316
Weights of high school football players, 119
Winning a game, 142
Winning times for men's and women's 100 -meter run, 580
WNBA most valuable player, 211
World Series, 200
Yards per carry, 317

## Work

Actuary salaries, 289, 556
Ages and career goals, 544
Architect salaries, 98, 427
Average salary of registered nurses, 7
Changing jobs, 77, 391
Civil engineer salaries, 340
College graduates working in jobs that do not require a college degree, 289
Company employment, 22
Computer hardware engineer salaries, 334
Construction worker salaries, 120
Earnings by educational attainment, 59, 430
Earnings of full-time workers, 410
Electrical engineer salaries, 126, 375
Employee salaries and ages, 508
Employee strike, 137
Employee training and accidents, 470
Employee wellness, 283
Employees' ages, 33
Employees' salaries, 4, 6, 50, 99, 200, 509, 511
Employment application, 15
Employment in a different state after graduation, 291
Employment status and educational attainment, 451, 547
Engagement in work, 30
Entry-level salaries, 444, 456
Fast-food employees, 33
First-year chemist salaries, 126
Forensic science technician salaries, 422
Graphic design specialist salaries, 401
Hiring applicants, 183
Hourly wages, 64, 79
Hours nurses work per week, 63
Important jobs, 328
Job growth, 10
Late for work, 213
Law firm salaries, 66
Length of employment and salary, 60
Librarian and library science teacher salaries, 521

Life insurance underwriter salaries, 316, 317
Locksmith salaries, 467
Marketing analyst salaries, 271
Mechanical engineer salaries, 371
Median and mean hourly wage, 505, 507
Medical care benefits, 226
Minimum wage, 7
MRI technologist salaries, 316, 317
Numbers of manufacturing employees, 101
Nurses becoming better professionals during the coronavirus pandemic, 391
Nursing supervisor salaries, 401
Organized union, 6
Overtime, 198, 288
Paid maternity leave, 411
Paycheck errors, 222
Physical therapist salaries, 289
Primary reason for career choice, 18
Product engineer salaries, 384
Public relations manager salaries, 556
Public school teacher salaries, 421
Registered nurse salaries, 493
Remote work, 76
Respiratory therapy technician hourly wages, 577
Salary offers, 94, 95
Security officer applicants, 360
Service employees in leisure and hospitality, 339
Sick days used by employees, 79
Software engineer salaries, 98, 427
Starting salaries, 82, 83, 84
Statistician salaries, 384, 567
STEM employment and mean wage, 505, 507
Stress at work, 3, 4
Teacher salaries, 65, 118, 520, 579
Time wasted at work, 562
Training program, 177
Travel time to work, 49, 62, 76
Unemployment, 3
Vacation days, 110
Wages by metropolitan area, 576
Waking times of employees, 338
Warehouse workers, 177
Web software development manager salaries, 271
Where people work and educational attainment, 538
Workdays missed due to illness or injury, 367
Workers by occupation, 144
Working from home, 165, 205
Working students, 391
Workplace cleanliness, 212
Workplace drug testing, 211
Workplace fraud, 126
Years of service, 53, 256

# Introduction to Statistics 


1.1

An Overview of Statistics
1.2

Data Classification
Case Study
1.3

Data Collection and Experimental Design

Activity
Uses and Abuses
Real Statistics-Real Decisions
History of Statistics-Timeline Technology

During 2020, the fastest-growing state in the United States was Idaho. In the same year, the Idaho cities of Meridian and Nampa were among the 10 fastest-growing cities in the United States.

## Whare Vou've Been

You are already familiar with many of the practices of statistics, such as taking surveys, collecting data, and describing populations. What you may not know is that collecting accurate statistical data is often difficult and costly. Consider, for instance, the monumental task of counting and describing
the entire population of the United States. If you were in charge of such a census, how would you do it? How would you ensure that your results are accurate? These and many more concerns are the responsibility of the United States Census Bureau, which conducts the census every decade.

## Where You're Going

In Chapter 1, you will be introduced to the basic concepts and goals of statistics. For instance, statistics were used to construct the figures below, which show the fastest-growing U.S. states from 2019 to 2020 by the percent increase in population and by the numerical increase in population, along with the regions where these states are located.

For the 2010 Census, the Census Bureau sent short forms to every household. Short forms ask all members of every household such things as their gender, age, race, and
ethnicity. Previously, a long form, which covered additional topics, was sent to about $17 \%$ of the population. But for the first time since 1940, the long form was replaced by the American Community Survey, which surveys more than 3.5 million households a year throughout the decade. These households form a sample. In this course, you will learn how the data collected from a sample are used to infer characteristics about the entire population.


Regions of the 25 States with Greatest Numerical Population Increases


### 1.1 An Overview of Staisitics

## What You Should Learn

## A definition of statistics

How to distinguish between a population and a sample and between a parameter and a statistic
How to distinguish between descriptive statistics and inferential statistics

For help with percents and reading graphs, see Integrated Review at MyLab® Statistics

## A Definition of Statistics ■ Data Sets ■ Branches of Statistics

## A Definition of Statistics

Almost every day you are exposed to statistics. For instance, consider the next two statements.

- "7 in 10 Americans believe the arts unify their communities, and 2 in 5 Americans have changed an opinion or perception based on an arts experience." (Source: Americans for the Arts)
- "Notably, $21 \%$ of $8-11$ year-olds have a social media profile." (Source: Smart Insights, Ltd.)

By learning the concepts in this text, you will gain the tools to become an informed consumer, understand statistical studies, conduct statistical research, and sharpen your critical thinking skills.

Many statistics are presented graphically. For instance, consider the figure shown below.


The information in the figure is based on the collection of data. In this instance, the data are based on the results of a science quiz given to 4464 U.S. adults.

## DEFINITION

Data consist of information coming from observations, counts, measurements, or responses.

The use of statistics dates back to census taking in ancient Babylonia, Egypt, and later in the Roman Empire, when data were collected about matters concerning the state, such as births and deaths. In fact, the word statistics is derived from the Latin word status, meaning "state." The modern practice of statistics involves more than counting births and deaths, as you can see in the next definition.

## DEFINITION

Statistics is the science of collecting, organizing, analyzing, and interpreting data to make decisions.


## Study Tip

A census consists of data from an entire population. But, unless a population is small, it is usually impractical to obtain all the population data. In most studies, information must be obtained from a random sample.

## Data Sets

There are two types of data sets you will use when studying statistics. These data sets are called populations and samples.

## DEFINITION

A population is the collection of all outcomes, responses, measurements, or counts that are of interest. A sample is a subset, or part, of a population.

A sample is used to gain information about a population. For instance, to estimate the unemployment rate for the population of the United States, the U.S. Bureau of Labor Statistics uses a sample of about 60,000 households.

A sample should be representative of a population so that sample data can be used to draw conclusions about that population. Sample data must be collected using an appropriate method, such as random sampling. When sample data are collected using an inappropriate method, the data cannot be used to draw conclusions about the population. (You will learn more about random sampling and data collection in Section 1.3.)

## EXAMPLE 1

## Identifying Data Sets

In a survey, 751 employees in the United States were asked how stressed they feel at work. Of the 751 respondents, 616 said that they feel at least a little stressed at work. Identify the population and the sample. Describe the sample data set. (Adapted from The Marlin Company)

## SOLUTION

The population consists of the responses of all employees in the United States. The sample consists of the responses of the 751 employees in the survey. In the Venn diagram below, notice that the sample is a subset of the responses of all employees in the United States. Also, the sample data set consists of 616 employees who said that they feel at least a little stressed at work and 135 who said that they do not feel stressed at work.

Responses of All Employees (population)


## TRY IT YOURSELF 1

In a survey of 1516 teens in the United States, 1228 said "mental health is a significant issue for young people in the U.S." Identify the population and the sample. Describe the sample data set. (Adapted from National 4-H Council)

Answer: Page A35
Whether a data set is a population or a sample usually depends on the context of the real-life situation. For instance, in Example 1, the population is the set of responses of all employees in the United States. Depending on the purpose of the survey, the population could have been the set of responses of all employees who live in California or who work in the health care industry.


## Study Tip

To remember the terms parameter and statistic, try using the mnemonic device of matching the first letters in population parameter and the first letters in sample statistic.


## Picturing the World

What is the cost of the U.S. Census? According to estimates, it has been escalating with each decade. The cost of the 1950 Census was approximately $\$ 91.5$ million. The most recent U.S. Census, taken in 2020, was estimated to cost a staggering $\$ 15.6$ billion. (Source: U.S. Census Bureau and U.S. Government Accountability Office)


What are some of the costs involved in taking a census?

Two important terms that are used throughout this course are parameter and statistic.

## DEFINITION

A parameter is a numerical description of a population characteristic.
A statistic is a numerical description of a sample characteristic.

It is important to note that a sample statistic can differ from sample to sample, whereas a population parameter is constant for a population. For instance, consider the survey in Example 1. The results showed that 616 of 751 employees surveyed feel at least a little stressed at work. Another sample may have a different number of employees who say they feel at least a little stressed at work. For the population, however, the number of employees who feel at least a little stressed at work does not change.

## EXAMPLE 2

## Distinguishing Between a Parameter and a Statistic

Determine whether each number describes a population parameter or a sample statistic. Explain your reasoning.

1. In the United States, a survey of about 9400 individuals aged 15 and over found that such individuals spent an average of 5.19 hours per day engaged in leisure and sports activities. (Source: U.S. Bureau of Labor Statistics)
2. The freshman class at a university has an average SAT math score of 514 .
3. In a random check of several hundred retail stores, the Food and Drug Administration found that $34 \%$ of the stores were not storing fish at the proper temperature.

## SOLUTION

1. Because the average of 5.19 hours per day is based on a subset of the population, it is a sample statistic.
2. Because the average SAT math score of 514 is based on the entire freshman class, it is a population parameter.
3. Because $34 \%$ is based on a subset of the population, it is a sample statistic.

## TRY IT YOURSELF 2

Determine whether each number describes a population parameter or a sample statistic. Explain your reasoning.
a. Last year, a small company spent a total of $\$ 5,150,694$ on employees' salaries.
b. In the United States, a survey of more than 1000 adults aged 65-80 found that $47 \%$ who report listening to loud or very loud music in their youth now report being hard of hearing. (Source: The Harris Poll)

Answer: Page A35

In this course, you will see how the use of statistics can help you make informed decisions. Consider the census that the U.S. government takes every decade. The Census Bureau attempts to contact everyone living in the United States. Although it is impossible to count everyone, it is important that the census be as accurate as it can be because public officials make many decisions based on the census information. Data collected in the census will determine how to assign congressional seats and how to distribute public funds.

## Not Online

U.S. adults who do not use the Internet by household income


## Study Tip

Throughout this course you will see applications of both branches of statistics. A major theme in this course will be how to use sample statistics to make inferences about unknown population parameters.

## Branches of Statistics

The study of statistics has two major branches: descriptive statistics and inferential statistics.

## DEFINITION

Descriptive statistics is the branch of statistics that involves the organization, summarization, and display of data.

Inferential statistics is the branch of statistics that involves using a sample to draw conclusions about a population. A basic tool in the study of inferential statistics is probability. (You will learn more about probability in Chapter 3.)

## EXAMPLE 3

## Descriptive and Inferential Statistics

For each study, identify the population and the sample. Then determine which part of the study represents the descriptive branch of statistics. What conclusions might be drawn from the study using inferential statistics?

1. A study of 1502 U.S. adults found that $18 \%$ of adults from households earning less than $\$ 30,000$ annually do not use the Internet, as shown in the figure at the left. (Source: Pew Research Center)
2. A study of 1000 U.S. $401(\mathrm{k})$ retirement plan participants found that the percentage who do not know how many years their retirement savings might last is $32 \%$. (Source: Charles Schwab \& Co., Inc.)

## SOLUTION

1. The population consists of the responses of all U.S. adults, and the sample consists of the responses of the 1502 U.S. adults in the study. The part of this study that represents the descriptive branch of statistics involves the statement " $18 \%$ of adults from households earning less than $\$ 30,000$ annually do not use the Internet." Also, the figure represents the descriptive branch of statistics. A possible inference drawn from the study is that the Internet has been made inaccessible to lower-income households.
2. The population consists of the responses of all U.S. $401(\mathrm{k})$ retirement plan participants, and the sample consists of the responses of the 1000 U.S. 401(k) retirement plan participants in the study. The part of this study that represents the descriptive branch of statistics involves the statement "the percentage [of U.S. 401(k) retirement plan participants] who do not know how many years their retirement savings might last is $32 \%$." A possible inference drawn from the study is that the amount of money a person needs for retirement is difficult to determine.

## TRY IT YOURSELF 3

A study of 513 respondents to an Internet-wide survey found that $97 \%$ of the respondents said music is important to them, and $83 \%$ of the respondents said they actively look for new music. (Source: Medium)
a. Identify the population and the sample.
b. Determine which part of the study represents the descriptive branch of statistics.
c. What conclusions might be drawn from the study using inferential statistics?

## Building Basic Skills and Vocabulary

1. How is a sample related to a population?
2. Why is a sample used more often than a population?
3. What is the difference between a parameter and a statistic?
4. What are the two main branches of statistics?

True or False? In Exercises 5-10, determine whether the statement is true or false. If it is false, rewrite it as a true statement.
5. A statistic is a numerical description of a population characteristic.
6. A sample is a subset of a population.
7. It is impossible to obtain all the census data about the U.S. population.
8. Inferential statistics involves using a population to draw a conclusion about a corresponding sample.
9. A population is the collection of some outcomes, responses, measurements, or counts that are of interest.
10. A sample statistic will not change from sample to sample.

Classifying a Data Set In Exercises 11-20, determine whether the data set is a population or a sample. Explain your reasoning.
11. The salary of each employee of an advertising firm
12. The amount of energy collected from every solar panel on a photovoltaic power plant
13. A survey of 250 members from an organized union of over 20,000 members
14. The annual revenue of each team in a pro sports league
15. The carbon monoxide levels of 12 of 49 people who escaped a burning building
16. The number of electoral college votes for each state in the U.S. and the District of Columbia
17. The number of guests in each room of a hotel
18. The amount spent by every tenth person cashing out at a store
19. The nationality of every person passing through a customs station
20. The precipitation amounts at 15 locations in a county

Graphical Analysis In Exercises 21-24, use the Venn diagram to identify the population and the sample.
21. Parties of Registered Voters

22. Meal Plan Choices of College Students

23. Ages of Adults in the United States Who Own Moter Vehicles


Ages of adults in the U.S. who own motor vehicles with more than two wheels
24. Incomes of Adults in Nevada


## Using and Interpreting Concepts

Identifying Data Sets In Exercises 25-34, identify the population and the sample. Describe the sample data set.
25. A survey of 1021 U.S. adults found that $45 \%$ have a favorable view of Cuba. (Source: Gallup)
26. A study of 227 U.S. infants was conducted to explore norms of the gut microbiomes of healthy infants. (Source: Scientific Reports)
27. A survey of 1500 U.S. adults found that $59 \%$ have never had a vaccine reaction. (Source: SingleCare)
28. A survey of 1028 U.S. adults found that $7 \%$ of respondents have never heard of organ and tissue donation. (Source: Research!America)
29. A survey of 2111 U.S. small business owners found that $54 \%$ oppose increasing the minimum wage. (Source: $C N B C$ )
30. A survey of 214 of the seniors graduating with a bachelor of science degree from a university found that $15 \%$ planned to obtain entry-level jobs in the health field.
31. A survey of 1001 U.S. adults found that $47 \%$ of respondents typically feel well rested on weekdays. (Source: National Sleep Foundation)
32. A survey of 366 automobile owners who purchased extended warranties found that $44 \%$ never used the warranty.
33. To gather information about starting salaries at companies listed in the Standard \& Poor's 500, a researcher contacts 74 of the 500 companies.
34. In a survey of 679 members of a local children's museum about parenting attitudes, 575 of the participants were female and 423 of the participants were parents of two or more children. (Source: University of California Press)

Distinguishing Between a Parameter and a Statistic In Exercises 35-42, determine whether the number describes a population parameter or a sample statistic. Explain your reasoning.
35. The average salary for 24 of a hospital's 82 registered nurses is $\$ 71,000$.
36. A survey of 919 college board members found that $89 \%$ think that their institution is a good place for members of racial and ethnic minorities. (Source: Association of Governing Boards of Universities and Colleges)
37. Sixty-two of the 97 passengers aboard the Hindenburg airship survived its explosion.
38. In January 2021, $54 \%$ of the governors of the 50 states in the United States were Republicans. (Source: National Governors Association)
39. In a survey of automobile owners, $6 \%$ said they had to change their engine control module at least once.
40. Voter registration records show that $47 \%$ of all voters in a county are registered as Democrats.
41. A survey of 1000 U.S. adults found that $79 \%$ think that the spread of infectious diseases is a major threat to the well-being of the United States. (Source: Pew Research Center)
42. In a recent year, the average math score on the ACT for all graduates was 20.2. (Source: ACT, Inc.)
43. Descriptive and Inferential Statistics Which part of the survey described in Exercise 31 represents the descriptive branch of statistics? What conclusions might be drawn from the survey using inferential statistics?
44. Descriptive and Inferential Statistics Which part of the survey described in Exercise 32 represents the descriptive branch of statistics? What conclusions might be drawn from the survey using inferential statistics?

## Extending Concepts

45. Identifying Data Sets in Articles Find an article that describes a survey.
(a) Identify the sample used in the survey.
(b) What is the population?
(c) Make an inference about the population based on the results of the survey.
46. Writing Write an essay about the importance of statistics for one of the following.

- A study on the effectiveness of a new drug
- An analysis of a manufacturing process
- Drawing conclusions about voter opinions using surveys

47. Exercise and Immunity A study showed the same level of T cell production in senior citizens who are amateur cyclists as in young adults, but a significantly lower level of T cell production in senior citizens who do not exercise regularly. Is it appropriate to infer that exercise stimulates T cell production? Explain. (Source: University of Birmingham)
48. Weight Loss and High Blood Pressure A study showed an association between intentional weight loss and a decreased risk of high blood pressure. Is it appropriate to infer from this study that weight loss causes a decreased risk of high blood pressure? Explain. (Source: European Association for the Study of Obesity)
49. Sleep and Student Achievement A study of college students showed that participants earned higher scores on quizzes and midterm exams with better sleep. (Source: The American Journal of Managed Care)
(a) Identify the sample used in the study.
(b) What is the population?
(c) Which part of the study represents the descriptive branch of statistics?
(d) Make an inference about the population based on the results of the study.

### 1.2 Data Classification

## What You Should Learn

How to distinguish between qualitative data and quantitative data
How to classify data with respect to the four levels of measurement: nominal, ordinal, interval, and ratio

Types of Data - Levels of Measurement

## Types of Data

When conducting a study, it is important to know the kind of data involved. The type of data you are working with will determine which statistical procedures can be used. In this section, you will learn how to classify data by type and by level of measurement. Data sets can consist of two types of data: qualitative data and quantitative data.

## DEFINITION

Qualitative data consist of attributes, labels, or nonnumerical entries.
Quantitative data consist of numbers that are measurements or counts.

## EXAMPLE 1

## Classifying Data by Type

The table shows a partial list of vulnerable, endangered, or critically endangered species and the approximate numbers of each species remaining. Which data are qualitative data and which are quantitative data? Explain your reasoning. (Source: World Wildlife Fund)

Vulnerable, Endangered, or Critically Endangered Species

| Common species name | Number remaining |
| :--- | :---: |
| African elephant | 415,000 |
| Black-footed ferret | 370 |
| Giant panda | 1864 |
| Indus river dolphin | 1816 |
| Javan rhinoceros | 60 |
| North Atlantic right whale | 400 |
| Sunda tiger | 400 |
| Tapanuli orangutan | 800 |
| Vaquita | 10 |

## SOLUTION

The information shown in the table can be separated into two data sets. One data set contains the common species names and the other contains the numbers remaining. The names are nonnumerical entries, so these are qualitative data. The numbers remaining are numerical entries, so these are quantitative data.

## TRY IT YOURSELF 1

The populations of several U.S. cities are shown in the table. Which data are qualitative data and which are quantitative data? Explain your reasoning. (Source: U.S. Census Bureau)

